

X and Y = R.V.'s
a and b = fixed numbers

Rules for combining and manipulating Means

* This is the 2nd half of 4.4 in book

μ_x = mean of X
 μ_{2x} = mean of 2x

Rule for multiplication and addition of one variable:

$$\mu_{a+bX} = a + b \cdot \mu_x$$

Rule for Combining X and Y together:

$$\mu_{X+Y} = \mu_x + \mu_y$$

Example:

- 1) Random variable X has mean of 6.2. Find the mean if we divide by 12 and add 3.

$$\mu_x = 6.2 \quad \mu_{\frac{1}{12}X+3} = \frac{1}{12}(\mu_x) + 3 = \frac{1}{12}(6.2) + 3 = \textcircled{3.52}$$

- 2) Random variable Y has mean of 3.4. Find the mean of X + Y.

$$\mu_y = 3.4 \quad \mu_{X+Y} = \mu_x + \mu_y = 6.2 + 3.4 = \textcircled{9.6}$$

- 3) Find μ_{2X+3Y}

$$\mu_{2X+3Y} = \mu_{2X} + \mu_{3Y} = 2 \cdot \mu_x + 3 \cdot \mu_y = 2(6.2) + 3(3.4) = \textcircled{22.6}$$

Rules for combining and manipulating Std. Deviations

X and Y = R.V.'s
a and b = fixed numbers

Notes:

- Variance = (standard deviation)² = σ^2
- ALWAYS... **WORK IN VARIANCES!!**

* find the σ^2 of what you want 1st, then take $\sqrt{\quad}$ to get to σ .

Rule for multiplication and addition of one variable:

* Adding or subtracting a constant to a variable...

$$\sigma_{a+bx}^2 = b^2 \cdot \sigma_x^2$$

(*note: "a" has no effect - it's ignored!
adding or subtracting a constant (a) doesn't change σ)

* Rule for Combining X and Y together:

$$\sigma_{x+y}^2 = \sigma_{x-y}^2 = \sigma_x^2 + \sigma_y^2$$

notice: + and -
are same!

σ_x = std. dev. of X

σ_{2x} = std. dev. of 2x

σ_x^2 = variance of X

Example:

- 1) Random Variable X has $\sigma = 3.1$.
Random Variable Y has $\sigma = 1.4$.

Find:

$$\sigma_{x+y} \Rightarrow \sigma_{x+y}^2 = \sigma_x^2 + \sigma_y^2 = (3.1)^2 + (1.4)^2 = 11.57 \Rightarrow \sqrt{11.57} = \boxed{3.401}$$

$\swarrow = \sigma_{x+y}^2$ $\swarrow \sigma_{x+y}$

$$\sigma_{x-y} = \sigma_{x+y} = \text{same as above! } \boxed{3.401}$$

$\swarrow \sigma_{2x+3}^2$ $\swarrow \sigma_{2x+3}$

$$\sigma_{2x+3} \Rightarrow \sigma_{2x+3}^2 = \sigma_{2x}^2 = 2^2 \sigma_x^2 = 2^2 (3.1)^2 = 38.44 \Rightarrow \sqrt{38.44} = \boxed{6.2}$$

$$\begin{aligned} \sigma_{3x+y-4} \Rightarrow \sigma_{3x+y-4}^2 &= \sigma_{3x+y}^2 = \sigma_{3x}^2 + \sigma_y^2 = 3^2 \sigma_x^2 + \sigma_y^2 \\ &= 3^2 (3.1)^2 + (1.4)^2 \\ &= 88.45 \leftarrow \sigma_{3x+y-4}^2 \\ &\Rightarrow \sqrt{88.45} \\ &= \boxed{9.405} \leftarrow \sigma_{3x+y-4} \end{aligned}$$

